Sensitive methods for estimating the anchoring strength of nematic liquid crystals on Langmuir-Blodgett monolayers of fatty acids

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The anchoring of the nematic liquid crystal N-(p-methoxybenzylidene)-p-butylaniline (MBBA) on Langmuir-Blodgett monolayers of fatty acids (COOHC $_nH_{2n+1}$) was studied as a function of the length of the fatty acid alkyl chain n (n = 15, 17, 19, 21). The monolayers were deposited onto glass plates coated with indium tin oxide, which were used to assemble sandwich cells of various thicknesses that were filled with MBBA in the nematic phase. The mechanism of relaxation from the flow-induced quasiplanar to the surface-induced homeotropic alignment was studied for the four aligning monolayers. It was found that the speed of the relaxation decreases linearly with increasing length of the alkyl chain n, which suggests that the Langmuir-Blodgett film plays a role in the phenomenon. This fact was confirmed by a sensitive estimation of the anchoring strength of MBBA on the fatty acid monolayers after anchoring breaking, which takes place at the transition between two electric-field-induced turbulent states, denoted as DSM1 and DSM2 (where DSM indicates dynamic scattering mode). It was found that the threshold electric field for the anchoring breaking, which can be considered as a measure of the anchoring strength, also decreases linearly as n increases. Both methods thus possess a high sensitivity in resolving small differences in anchoring strength. In cells coated with mixed Langmuir-Blodgett monolayers of two fatty acids (n = 15 and n = 17) a maximum of the relaxation speed was observed when the two acids were present in equal amounts. This observation suggests an efficient method for controlling the anchoring strength in homeotropic cells by changing the ratio between the components of the surfactant film.

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I. INTRODUCTION

For the operation of liquid crystal displays and devices the alignment of the liquid crystal (LC) plays a vital role. In the absence of an external electric or magnetic field (fieldfree condition) the liquid crystal alignment is entirely dictated by the LC/substrate interactions. These interactions have been the subject of intensive study for more than two decades with surface anchoring being one of the highlights of the surface physics of liquid crystals. Although the LC/ substrate interactions are to a large extent understood, the lack of sensitive and reliable techniques for measuring the anchoring strength is an obstacle to fast progress of our knowledge in this field.

There are various techniques for measuring the anchoring strength [1-3]. In general, they can be divided in two major groups depending on whether the measurements were carried out in a field-free condition or not. One of the most frequently and widely used methods is the Fréedericksz transition [2]. Although it gives satisfactory results, in some cases it is not sensitive enough to resolve small differences in anchoring strength.

The effort in the development of liquid crystal displays has been focused, generally speaking, on improving the image contrast, the resolution, and the number of gray levels, as well as on increasing the size of the display and shortening the response time. Recently [4,5], the so called vertical alignment (VA) mode display has begun to attract the interest of researchers and engineers for two reasons. First, the homeotropic (vertical) alignment of the liquid crystal required by the VA mode can be easily controlled by an electric field, due to the weak anchoring conditions. Second, the contrast is very high and the response time is short. To realize the VA mode, however, it is necessary to align the liquid crystal homeotropically, i.e., with the nematic director perpendicular to the confining substrate. Also, the homeotropic anchoring strength is an important parameter that influences the device performance.

There are a number of methods for obtaining homeotropic alignment [6]. Among them, the most used is that of treating the substrate with a surfactant. It is known that very densely packed surfactant layers do not give homeotropic alignment of good quality. A looser packing of the surfactant molecules usually gives good homeotropic alignment since it allows a certain degree of penetration (interdigitation) of the liquid crystal molecules in the surfactant layer [7,8]. Homeotropic alignment obtained with different agents differs not only in the degree of uniformity, but also in the magnitude of the strength of the liquid crystal anchoring, which varies between 10^{-5} and 10^{-6} J m⁻² (weak anchoring).

In this work the anchoring of MBBA [*N*-(*p*-methoxybenzylidene)-*p*-butylaniline] on Langmuir-Blodgett (LB) monolayers of fatty acids (COOHC_nH_{2n+1}) is studied as a function of the length n (n=15,17,19,21) of the

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TABLE I. Long chain fatty acids used in this experiment.

Common name	Formula	Abbreviation
Palmitic	C ₁₅ H ₃₁ COOH	C16
Stearic	C ₁₇ H ₃₅ COOH	C18
Arachidic	C ₁₉ H ₃₉ COOH	C20
Behenic	C ₂₁ H ₄₃ COOH	C22

fatty acid alkyl chain. Generally, the nematic liquid crystal anchoring is characterized by two parameters w_{θ} and w_{φ} , the polar and azimuthal anchoring strength, respectively. Here only w_{θ} will be considered and we will refer to it as w.

In previous studies [9] we have shown that the nematic liquid crystal (NLC) capillary flow has a strong impact on the surfactant LB monolayer. The LB molecules are oriented in the azimuthal direction of the flow with a large pretilt, which results in a quasiplanar NLC alignment with splaybend deformation and preferred orientation along the flow direction [9–11]. Once the flow ceases the LB film relaxes to the equilibrium orientation in which the LB molecules present a tilt (about 40°) isotropically distributed in the plane of the cell, which induces homeotropic alignment in the NLC bulk. Here we will show that the dynamics of this process depend on the length of the surfactant molecules. Also, in [12] we have shown that above a certain electric field threshold a turbulence-to-turbulence (DSM1-DSM2 where DSM indicates dynamic scattering mode) transition occurs in MBBA, which is related to breaking of the anchoring. The threshold was found to be proportional to the anchoring strength. (about 10^{-6} Jm^{-2}), being thus a measure of it. Here we will show that this turbulence-to-turbulence transition is very sensitive to w, and it can resolve even very small differences due to the use of slightly different surfactants. Since homeotropic alignment is generally weak these differences can be extremely small. In this context it is important to underline that the Fréedericksz transition method, the most widely used method for evaluating w, does not possess the same sensitivity.

II. EXPERIMENT AND RESULTS

A. Film preparation

The long chain fatty acids used in this experiment are listed in Table I. They were spread from chloroform solutions on the surface of ultrapure Milli-Q water in a LB trough held in a clean room. The monolayers at the air/water interface were characterized by surface-pressure compression isotherms, which are shown in Fig. 1. Three condensed phases were observed for all substances, whose characteristics are listed in Table II. We chose to deposit the LB films in the L'_2 phase, where the molecules are almost upright and still the monolayers are far from collapse [13]. Also, the monolayers were deposited at the same area per molecule (0.2 nm²), in order to have the same surface density of molecules on the plates.

We also deposited mixed monolayers of C18 and C22 in different proportions. The miscibility of these two fatty acids



FIG. 1. Surface pressure versus area per molecule isotherms (20 °C) of the fatty acids listed in Table I. We can distinguish the liquid (L_2), the liquid-condensed (L'_2), and the solid (S) phases (see Table II for phase characteristics). The dashed line indicates the deposition conditions: phase L'_2 and the same area per molecule (0.2 nm²).

at the air/water interface has been studied elsewhere [14]. The isotherms are shown in Fig. 2. The mixed monolayers were deposited at the fixed surface pressure of 20 mN m⁻¹. The transfer ratio was always 1.

We used glass plates coated with indium tin oxide (ITO), previously carefully cleaned in a clean room environment.

B. Alignment dynamics

The LB coated plates were used to assemble sandwich cells (Fig. 3) of various thicknesses. The cells were filled with MBBA in the nematic phase (room temperature). During filling the NLC adopts a bend-splay-deformed quasiplanar alignment with preferred orientation along the filling direction. As soon as the flow stops, homeotropic domains nucleate in the cell and expand until the whole sample becomes homeotropic. The role of the LB monolayer has been discussed in [9,10]: during the filling process the chains are distorted by the flow, and relax to the equilibrium position once the flow has ceased (Fig. 4).

A time sequence of pictures of a homeotropic domain expanding in the quasiplanar structure is shown in Fig. 5. The pictures refer to a cell whose plates were coated with a monolayer of C18. The procedure was repeated for the four aligning fatty acids listed in Table I and the speed of expansion of the homeotropic domains was found to depend on the length of their alkyl chains and on the cell thickness, as shown in Fig. 6.

TABLE II. Condensed monolayer phases for fatty acids (after Petty [13]).

Phase	Name	Characteristics
L_2	liquid condensed	tilted molecules
L'_2	liquid condensed	almost upright molecules;
		same compressibility as L_2
S	solid	upright molecules; high collapse pressure;
		less compressible than L_2 and L'_2



FIG. 2. Surface pressure versus area per molecule isotherms $(20 \,^{\circ}C)$ of the C18-C22 mixed monolayers. The proportions of the two compounds are specified.

The dynamics of the process is governed by surface and bulk effects. Here we present a simple model in which only two contributions are taken into account, namely, a rapid relaxation in the boundary LB monolayer (whose characteristic time is τ_s) followed by the elastic relaxation of the splay-bend deformation in the bulk (whose characteristic time is τ_b). The total relaxation time τ is given by

$$\frac{1}{\tau} = \frac{1}{\tau_{\rm s}} + \frac{1}{\tau_{\rm b}}.\tag{1}$$

For a (small) deformation θ (see Fig. 4) the surface process is determined by the balance between the anchoring, elastic, and surface viscosity forces and reads [1]

$$K\frac{\partial\theta}{\partial z} + w\,\theta = \eta\,\frac{\partial\theta}{\partial t},\tag{2}$$

where *K* is the characteristic elastic constant of the splaybend deformation in the one-constant approximation, *w* is the anchoring strength, and η is the surface viscosity [15]. The characteristic time τ_s is given by

$$\tau_{\rm s} = \frac{2w\,\eta}{w^2 + K^2\beta^2},\tag{3}$$

where β^{-1} is a characteristic length given by

$$\beta^{-2} = \frac{K^2 - dKw}{w^2},\tag{4}$$



FIG. 3. Cross section of a cell.



FIG. 4. Left: during filling the LB monolayer is affected by the flow and the NLC is quasiplanarly aligned with bend-splay deformation. Right: as soon as the flow ceases the elastic deformation and the LB film both contribute to the relaxation to the homeotropic alignment.

and *d* is the cell thickness. In the case of weak anchoring $K/wd \ge 1$ and thus $\beta^{-1} = K/w$, the extrapolation length [2]. In this case the surface relaxation time becomes

$$\tau_{\rm s} = \frac{\eta}{w}.\tag{5}$$

The bulk process is determined by the balance between the elastic torque and the bulk viscous torque and reads [1]

$$K\frac{\partial^2\theta}{\partial z^2} = \gamma \frac{\partial\theta}{dt},\tag{6}$$

where γ is the bulk viscosity. The characteristic time of the bulk relaxation is then [10]

$$\tau = \frac{\gamma d^2}{\pi^2 K}.\tag{7}$$

In our experiment we measured directly the speed with which the homeotropic domains expand in the quasiplanar state, i.e., the speed with which the quasiplanar domain relaxes to homeotropic. The speed of the surface (bulk) relaxation v_s (v_b) is inversely proportional to the surface (bulk) relaxation time, i.e., $v_s \propto \tau_s^{-1}$ ($v_b \propto \tau_b^{-1}$). Thus, using Eq. (1), the total speed of relaxation $v = v_s + v_b$, is given by

$$v \propto \frac{w}{\eta} + \frac{K\pi^2}{\gamma d^2}.$$
 (8)

Due to the selective adsorption of ions present in the NLC bulk at the surface [16,17], w depends on the cell thickness. This ionic charge attracts ions of the opposite charge and a double layer of charges is formed that depends only on the substrate and on the NLC used. As a consequence, a surface electric field is created, which extends in the bulk over the Debye screening length λ_D . For symmetry reasons the field is normal to the substrate and has an orienting effect on the NLC through the coupling to the dielectric anisotropy. The anchoring strength thus appears to be thickness dependent because the amount of ions present in the liquid crystal depends on the sample volume, which is proportional to the cell thickness d. This effective anchoring strength can be written as [17]



FIG. 5. Cell between crossed polarizers. A homeotropic domain (dark) expands in the quasiplanar domain. LB aligning layer, C18; cell thickness, 12.5 μ m; time interval, 30 s.

$$w = w_{\rm R} + \frac{|\Delta\varepsilon|\lambda_{\rm D}}{2\varepsilon^2\varepsilon_0}\sigma^2,\tag{9}$$

where the flexoelectric effect has been neglected. In Eq. (9) $w_{\rm R}$ is the Rapini-Papoular anchoring strength [18] which does not depend on the cell thickness. $\Delta \varepsilon$ is the dielectric anisotropy, ε is the average dielectric constant of the liquid crystal, and ε_0 is the vacuum dielectric constant. σ is the electric charge density adsorbed at the surface,



FIG. 6. Speed of expansion of the homeotropic domains as a function of the cell thickness *d* for the four LB aligning layers. The symbols are the experimental values and the lines are fits to the function in Eq. (13) below. The fitting parameter v_s depends on the LB aligning layer, while *B* was found to be essentially the same for all LB layers ($B = 400 \ \mu \text{m}^3 \text{ s}^{-1} \pm 40 \ \mu \text{m}^3 \text{ ms}^{-1}$).

$$\sigma = \Sigma \frac{d}{d + 2\lambda_{\rm D}},\tag{10}$$

where Σ depends on the conductivity of the liquid crystal and on the characteristics of the surface.

Using Eqs. (9) and (10), Eq. (8) becomes

$$v \propto \frac{w_{\rm R}}{\eta} + \frac{C}{\eta} \left[\frac{d}{d+2\lambda_{\rm D}} \right]^2 + \frac{K\pi^2}{\gamma d^2},\tag{11}$$

where

$$C = \frac{|\Delta\varepsilon|\lambda_{\rm D}}{2\varepsilon^2\varepsilon_0}\Sigma^2 \tag{12}$$

is a constant characteristic of the liquid crystal and the substrate. Generally $\lambda_D \ll d$ [16] and the second term on the right-hand side of Eq. (11) varies very little with *d* as compared to the third term. Thus, the *surface speed* v_s can be considered essentially constant with respect to the *bulk speed* v_b in the range of cell thickness used in this work. Eq. (11) can thus be rewritten as

$$v = v_s + Bd^{-2},$$
 (13)

where $v_s = (w_R + C)/\eta = \text{const}$ and *B* is a proportionality factor that depends on *K* and γ .

The data in Fig. 6 where fitted to the function in Eq. (13) and the fits are shown in the figure. The fitting parameter v_s was found to depend on the LB aligning monolayer, as shown in Fig. 7, which is in agreement with our interpretation of it as characteristic of the surface. The fitting parameter *B* was found to be essentially constant within the error bars ($B=400\pm40 \ \mu m^3 s^{-1}$), independent of the aligning monolayers. The surface relaxation is faster for shorter chains, and seems to follow a linear relation with the number of carbon atoms in the chain. Moreover, the quality of the homeotropic alignment itself is higher for shorter chains. These two observations together suggest that the anchoring of MBBA is quite sensitive even to small differences in the length of the surfactant. For instance, the anchoring strength



FIG. 7. *Surface speed* of expansion of the homeotropic domains as a function of the aligning monolayer chain length. The agreement with a linear decrease of v_s with increasing length of the chain is very good.

is expected to be affected by the presence of chains of different lengths in the same monolayer.

The relaxation process was also studied in cells of fixed thickness (15 μ m) coated with mixed LB films of C18 and C22 in different ratios. Figure 8 shows the speed of relaxation of the homeotropic domains as a function of the percentage of C18 in the LB aligning monolayer. The relaxation is faster for the mixed layers in which the proportions of the two compounds are similar. In particular, the highest speed is obtained for the 50:50 mixture. Also, in this case the quality of the homeotropic alignment was higher in those cells where the relaxation process was faster.

C. Anchoring strength

The anchoring strength of MBBA on the fatty acid LB monolayers has been measured with the Fréedericksz transition method [2]. MBBA possesses negative dielectric anisotropy and thus a vertical electric field destabilizes MBBA's homeotropic alignment. Homeotropic alignment appears dark between crossed polarizers. Above a certain electric field threshold (Fréedericksz transition threshold) the molecules in the bulk are tilted by the electric field and some light is transmitted through the crossed polarizers. Here we defined as threshold field E_t the one at which 20% of the saturated value of the transmitted light intensity was reached. The anchoring strength *w* can then be calculated as [11,12]:



FIG. 8. Speed of expansion of the homeotropic domains as a function of the percentage of C18 in the mixed C18-C22 aligning LB monolayer. Cell thickness, 15 μ m.



FIG. 9. Anchoring strength of MBBA on the four fatty acid LB monolayers. The anchoring is weak [12] and the rather large error of the method does not allow one to resolve small differences.

$$w = qK \tan\left(\frac{qL}{2}\right)$$
 with $q = E_t \sqrt{\frac{|\Delta\varepsilon|\varepsilon_0}{K}}$. (14)

In Fig. 9 the dependence of w on the cell thickness is presented. Because of the weak anchoring the small differences in anchoring strength due to the different aligning layers cannot be resolved using this method.

The data in Fig. 9 are fitted very well by Eq. (9) (in Fig. 9 only the fit for the C16 data is shown). $w_{\rm R}$ and Σ are the fitting parameters. Σ was found to be (1.3 $\pm 0.3) \times 10^{-4}$ C m⁻² independent of the cell thickness, but $w_{\rm R}$ was found to decrease with increasing chain length of the surfactant, as shown in Fig. 10. This dependence recalls that of the relaxation speed of the homeotropic alignment (Fig. 7): the agreement with a linear decrease of $w_{\rm R}$ with increasing length of the chain is rather good.

D. Anchoring breaking

Recently [12] we have shown that an alternative method for measuring/comparing anchoring strengths is the mechanism of anchoring breaking due to the onset of an electricfield-induced turbulence-to-turbulence transition in the sample. Above the Fréedericksz transition threshold initially homeotropic MBBA (aligned by a fatty acid monolayer) be-



FIG. 10. Rapini-Papoular anchoring strength of MBBA on fatty acids. The trend is similar to that of the relaxation speed of the homeotropic alignment: the agreement with a linear decrease of w_R with increasing length of the chain is rather good.



FIG. 11. DSM2 domains expand in the DSM1 turbulent state. Note the circular form of the DSM2 domains, due to absence of a preferred alignment direction in the plane of the cell because of the initial homeotropic alignment [12,19] (in planar cells they expand faster in the rubbing direction [20,21]).

comes essentially quasiplanar. Increasing the field above the Fréedericksz threshold one observes first modulated structures (William rolls [1]), then their destabilization, and then the transition to a weakly turbulent state, called DSM1 (dynamic scattering mode 1). These electric-field-induced instabilities do not affect the anchoring of MBBA on the fatty acid monolayer, and the homeotropic alignment is immediately restored once the electric field is switched off [12]. On increasing the electric field further above the DSM1 threshold, one observes the transition to another turbulent state, denoted as DSM2: domains of DSM2 nucleate in the nematic



layer, which is in the DSM1 state, and expand over the whole sample area in the form of circular domains [12,19] (Fig. 11). In [12] we demonstrated that the DSM1-to-DSM2 transition is due to the breaking of the surface anchoring: on switching off the electric field above the DSM2 transition, the homeotropic alignment is not immediately restored. Instead, the sample is in a metastable quasiplanar state which relaxes to homeotropic as the flow-induced quasiplanar state does (in the form of circular homeotropic domains that expand until the whole sample becomes homeotropic again). Thus, the electric field threshold of DSM2 is proportional to the anchoring strength and can be considered as a measure of it.

In Fig. 12 the electric field threshold for DSM2, E_{DSM2} , in MBBA cells is shown as a function of the cell thickness for the four fatty acid LB aligning layers. There is a clear dependence on the nature of the LB monolayer, which demonstrates how sensitive this method is in resolving the small differences arising from the different thicknesses of the aligning monolayers. Since the threshold for DSM2 is proportional to the anchoring strength, the data were fitted with a function proportional to the anchoring strength in Eq. (9):



FIG. 12. Threshold for the onset of the DSM2 turbulent state for MBBA on fatty acid LB monolayers as a function of the cell thickness. E_{DSM2} depends on the length of the alkyl chain of the fatty acid: the differences in anchoring strength of MBBA on the different LB monolayers are therefore resolved. The lines are fits to the function in Eq. (9).

FIG. 13. The fitting parameter Cw_R is proportional to w_R and thus decreases linearly with increasing length of the alkyl chain.



FIG. 14. Threshold for the onset of the DSM2 turbulent state for MBBA on fatty acid LB monolayers as a function of the length of the fatty acid alkyl chain, for different cell thicknesses. E_{DSM2} decreases linearly with increasing chain length.

where *C* is a constant of proportionality. The fitting parameter Cw_R is proportional to w_R and thus decreases linearly with increasing length of the alkyl chain (Fig. 13) like w_R (Fig. 10).

From the fits it is possible to extrapolate the value of E_{DSM2} as a function of the LB chain length for different cell thicknesses, which is plotted in Fig. 14. E_{DSM2} decreases linearly with increasing chain length, like v_s and w_R .

III. DISCUSSION AND CONCLUSIONS

Whereas the present knowledge about alignment of liquid crystals (especially nematics) may be considered as sufficient for achieving a desired kind of alignment, the tuning of the anchoring strength is a very difficult task, if not impossible. The difficulties in controlling the anchoring strength arise not only from the lack of proper aligning materials, but also from the lack of sensitive enough methods to resolve small variations in anchoring strength.

In this work, two methods for estimating the anchoring strength of homeotropically aligned NLCs on LB monolayers of fatty acids have been presented. One of them is fieldfree, whereas in the other one an external electric field is necessary.

In the field-assisted method, the threshold for the onset of the DSM2 turbulent state can be interpreted as a measure of the anchoring strength, because above that threshold the anchoring of the liquid crystal to the substrate is broken. For a fixed cell thickness E_{DSM2} decreases linearly with increasing length of the surfactant chain. The "surface speed" of relax-



FIG. 15. Alignment of MBBA on mixed LB monolayers of C18 (white) and C22 (gray). Some of the LC molecules (gray) penetrate into the region of the surfactant, but some of them (black) are aligned because of the difference in the lengths of the alkyl chains, about 0.4–0.5 nm (interdigitation).

ation from flow-induced quasiplanar to surface-induced homeotropic alignment also decreases linearly with increasing length of the surfactant chain, and can thus also be interpreted as a measure of the anchoring strength. The two methods not only present quite a high sensitivity, as they can resolve very small differences in anchoring strength due to the use of slightly different surfactants, but also give independent and consistent results.

In cells treated with mixed C18-C22 LB monolayers it was found that the relaxation speed, and thus the anchoring strength, strongly depends on the mixture used and it is correlated with the quality of the homeotropic anchoring. In particular, the relaxation speed is maximum for similar concentrations of the two fatty acids in the mixed monolayer. In this case, in fact, the LC is aligned not only by penetration into the surfactant chain region, but also by penetration into the "holes" created by the differences in chain length (interdigitation). A schematic picture is shown in Fig. 15. This suggests a way of "tuning" the anchoring strength: w can be changed by varying the ratio of the components of the LB film, and thus the density of "holes." That the LB film density influences the anchoring of nematics is known [22], but the phenomenon of interdigitation has not yet been addressed.

In conclusion, the methods presented in this work make it possible to carry out detailed studies on the anchoring of nematic liquid crystals on surfactants. Their sensitivity allows the use of a great variety of surfactants or, more generally, materials that induce homeotropic alignment. On the basis of the results obtained new theoretical models can be developed in order to reach a deeper understanding of the microscopic LC-surfactant interactions.

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